

2017:00656- Unrestricted

Report

Impact of changing climate on infrastructure in Longyearbyen: stability of foundations on slope terrain – Case study

Project Report 2017

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SINTEF Building and Infrastructure Rock and Soil Mechanics 2017-11-22



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KEYWORDS: Climate change Infrastructure Longyearbyen Active layer Slope stability Pile foundations

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VERSION 01 AUTHOR(S) Vared Bekele

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CLIENT(S)

Svalbard Environmental Protection Fund Longyearbyenn Lokalstyre Store Norske Spitsbergen Kulkompani AS

PROJECT NO. 102015174

ABSTRACT

Climate data over the past couple of years show that record-breaking temperature and precipitation are observed in Svalbard. It is believed that global climate warming will impose serious impact on infrastructure. In this study, an assessment of vulnerability of selected infrastructures in Longyearbyen due to projected changes in climate is performed. Changes in ground temperature are investigated using analytical and numerical approaches. The results show that active layer thicknesses will increase and the underlying permafrost gets warmer. These changes significantly affect the stability of slopes and the bearing capacity of existing infrastructure and this is shown through further numerical studies. Slope angle, location of pile on slope and pile material are considered in the evaluations. Timber piles are especially affected where the capacity reduces due to aging. Further detailed and specific studies are required for individual assessment of slopes and foundations. The study also highlights the importance of considering climate change in the design of new infrastructure.

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REPORT NO. 2017:00656

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NUMBER OF PAGES/APPENDICES: 39



Document history

VERSIONDATEVERSION DESCRIPTION1.02017-11-22Project Report

Table of contents

1	1 Introduction		
	1.1	Background 4	
	1.2	Description of the Initiative 4	
	1.3	Infrastructures for the Study 5	
2	Grou	nd Thermal Regime6	
	2.1	Longyearbyen Air Temperatures 6	
		2.1.1 Existing Data and Forecast6	
		2.1.2 Air Freezing and Thawing Indices7	
	2.2	Active Layer: Analytical Calculations8	
	2.3	Ground Temperature: Numerical Simulations10	
3	Slope	Stability Evaluation15	
	3.1	Location of Slope	
	3.2	Effect of Climate Change 19	
	3.3	Sensitivity to Material Parameters	
4	Later	ally Loaded Piles on a Slope21	
	4.1	Solifluction	
	4.2	Theory of Laterally Loaded Piles 22	
	4.3	p-y Curves for Frozen Soil	
	4.4	Analytical Calculations 23	
		4.4.1 Effect of Climate Change	
		4.4.2 Effect of Slope Angle	
		4.4.3 Effect of Pile Diameter	
	4.5	Finite Element Simulations	
		4.5.1 Effect of Climate Change	
		4.5.2 Effect of Pile Location	
		4.5.3 Effect of Pile Material	
	4.6	Bending Capacity of Piles	
5	Sumr	nary, Conclusions and Outlook36	
Refe	rences		



1 Introduction

1.1 Background

The last years exhibit record-breaking values of air temperatures and amount of precipitation in Svalbard. Several severe events caused by environmental hazards took place in Longyearbyen in the last decade and the last few years in particular. One may relate such events as manifestation of a changing climate.

It is believed that global climate warming will impose serious impact on infrastructure in the arctic. Assessment of impact of changing climate on arctic infrastructures was performed in [1]. Authors of the latter assessment point out increased concerns related to the impact of projected climate change on arctic infrastructure. In particular, projected climate change may "increase the environmental stresses structures are exposed to; affect geohazards and the impacts of extreme events."

Svalbard Archipelago has experienced warming during 20th century, especially in the last three decades [2]. Evaluations of future climate suggest significant air warming, increase of precipitation, and increasing storm frequency [3-5]. The latest observations at Svalbard airport show air temperatures and precipitations at values of much higher than normal. Moreover, July 2016 was the single warmest month ever recorded; [6].

Increase in air temperatures leads to degradation of permafrost. Consequences of permafrost degradation according to [7] consist in increased thickness of the active layer, warming of permafrost at depth, and permafrost thawing. One can expect that the latter phenomena will lead to decrease of bearing capacity of foundations based on permafrost. Assessment performed by [8] showed that theoretical pile capacity in Longyearbyen decreased insufficiently (by 12.5%) in the period 1977–2007. However, it is relevant to assess how existing foundations in Longyearbyen will withstand to projected climate change.

Increased intensity of rainfall may increase the risk for landslides in ice-rich permafrost [9], which may be facilitated by increase of thawing depths of the ground due to increased summer air temperatures. Solifluction, i.e. slow (with rates of few cm/yr) downslope flow of saturated unfrozen earth materials (in summertime, when the upper layer of permafrost is thawed), affects serviceability of foundations in Longyearbyen. Action of solifluction was not taken into account for the design of foundations for many buildings in Longyearbyen, [10]. Several issues related to solifluction can be observed today. An important question to be answered is "Will existing infrastructure on slope terrain hold up in new conditions taking place due to climate change?"

1.2 Description of the Initiative

The initiative suggests performing an assessment of vulnerability of selected infrastructures in Longyearbyen due to projected changes in climate. It is suggested to perform an assessment of bearing capacity and serviceability analysis of pile foundations (taking into account the solifluction) of existing buildings on slope terrain.

The assessment is needed for managing the existing buildings and for future areal planning. Particular reasons are the following:

• Significant number of buildings in slope terrain in Longyearbyen are experiencing issues due to slope processes (solifluction). Therefore, an assessment is needed in order to foresee when and what kind of interaction has to be done in order maintain functionality of existing buildings.

PROJECT NO.	REPORT NO.	VERSION	4 of 39
102015174	2017:00656	01	4 01 3 9



• The areas with slope terrain should not be excluded from the planning of residential buildings and other infrastructures, but foundation solutions shall be obtained to fulfil requirements of serviceability (requirements to acceptable settlements and displacements).

1.3 Infrastructures for the Study

Initially suggested area [11] and several buildings and slope areas identified as suitable for the research [12] are presented on Figure 1.



Figure 1. Buildings and areas identified for present study.

Building at Vei 232.16 and area up slope was selected by the participants of the kick-off meeting as preferable study object within the project. This slope may be considered to be in "isolated solifluction conditions", i.e. on minimal artificial changes (cut profiles or berms) are introduced into this slope.

Field work was conducted at the preferable study area in early March 2017.



2 Ground Thermal Regime

The ground thermal regime is investigated based on existing temperature data and forecasts. The air temperature data is used to calculate the progression in the air thawing index and the active layer thickness. Analytical calculations and numerical simulations are performed to study the expected evolution of ground temperatures based on the temperature forecasts. The ground temperature calculated here will serve as an input for the calculation of the bearing capacity of pile foundations in later sections.

2.1 Longyearbyen Air Temperatures

The air temperature data for Longyearbyen based on existing data and forecasts is presented here. Parameters relevant for studying ground thermal regimes are determined based on these data.

2.1.1 Existing Data and Forecast

Air temperature data and forecasts for Longyearbyen are obtained from The Norwegian Meteorological Institute through personal communications with Rasmus E. Benestad. Climate projections for Svalbard courtesy of The Norwegian Meteorological Institute and other collaborators are reported in publications such as [4] and [5].



Figure 2-1: Longyearbyen air temperature progression from existing data and downscaled forecast in terms of seasonal mean values. The forecast is corresponding to RCP8.5. Data courtesy of Rasmus E. Benestad through internal communication.

The downscaled seasonal mean temperatures for Longyearbyen based on RCP8.5 are presented and used here. RCP8.5 is the scenario with highest greenhouse gas concentrations, which provides the highest projecting of global warming increase. The seasonal mean temperatures and standard deviations are

PROJECT NO.	REPORT NO.	VERSION	6 of 39
102015174	2017:00656	01	0 01 3 9



obtained and these are believed to provide more robust estimates as the mean is better estimated for a seasonal sample than for a monthly or daily sample. The seasonal means and standard deviations can be used to predict daily temperatures whenever necessary, as will be discussed in subsequent sections.

The air temperature data and forecast are available for the period from 1900 - 2100. The upper and lower bounds are estimated assuming a normal distribution for the temperature; see for example [4]. The evolution of the seasonal mean temperature, including the estimated upper and lower bounds, are shown in Figure 2-1.

2.1.2 Air Freezing and Thawing Indices

The air thawing and freezing indices are defined as the aggregate durations (usually reported in number of days) when the air temperatures are below and above the freezing temperature; see [13]. The air freezing index (I_{af}) is an important parameter for the estimation of the maximum depth of ground-frost penetration depth. The air thawing index (I_{at}) is used for the prediction of permafrost distribution and for the estimation of thaw depth in frozen ground.



Figure 2-2: Air freezing indices based on seasonal mean temperatures (top) and inferred daily temperatures (bottom).

PROJECT NO.	REPORT NO.	VERSION	7 of 39
102015174	2017:00656	01	70133



The air freezing and thawing indices are calculated based on the temperature data and forecast presented in Figure 2-1. The air freezing indices based on seasonal means and inferred daily temperatures are shown in Figure 2-2. It can be seen from the figure that all seasonal mean temperatures beyond ca. 2080 are all positive. Similarly, the air thawing indices based on seasonal mean and inferred daily temperatures are shown in Figure 2-3. The daily temperatures are inferred from the seasonal means and standard deviations by assuming a normal distribution. Both results are shown for the year periods from 2000 - 2100.



Figure 2-3: Air thawing indices based on seasonal mean temperatures (top) and inferred daily temperatures (bottom).

2.2 Active Layer: Analytical Calculations

The active layer is the soil above permafrost that freezes and thaws seasonally. The thickness of the active layer is governed by soil temperature which is a product of heat exchange between the atmosphere (air temperature) and ground surface; [14]. The thickness of the active layer is affected by several factors. Some of the broader factors include solar isolation patterns, latitude of the location, elevation of the area and proximity to glaciers and water bodies. Local factors that govern the active layer thickness

PROJECT NO.	REPORT NO.	VERSION	8 of 39
102015174	2017:00656	01	0 01 39

include amount of snow cover (which depends on amount of precipitation, temperature, wind patterns, ground surface morphology), vegetation cover and soil type.

There are a number of analytical approaches which can be used to calculate the thickness of the active layer during seasonal freezing and thawing. Some of these analytical methods include the Modified Berggren Equation, the Neumann Equation and the Stefan Solution. We apply the Stefan Solution here to estimate the active layer thicknesses.

The details of the Stefan Solution can be referred from [13]. It is assumed in this method that the temperature distribution in the thawed soil is linear while the temperature in the frozen zone is ignored. In addition, the soil properties in the frozen and thawed zones are assumed to be homogeneous and independent of temperature. It is also assumed that the latent heat is liberated at 0°C in the thawing soil. Based on these assumptions, the thawing depth z_{th} for a frozen soil mass subjected to a step increase in temperature at the surface can be calculated from the expression

$$z_{th} = \sqrt{\frac{2\lambda_u T_s t}{L}}$$
(2.1)

where λ_u is the unfrozen soil thermal conductivity, T_s is the applied constant surface temperature, t is time and L is the volumetric latent heat of the soil. The applied constant surface temperature can be obtained from

$$T_s = \frac{I_{st}}{t} \tag{2.2}$$

where I_{st} is the ground surface thaw index expressed as a function of the air thawing index I_{at} as

$$I_{st} = n_t I_{at} \tag{2.3}$$

where n_t is called the thawing *n*-factor. This factor is used to consider the difference between air temperatures and ground surface temperatures as this have been shown to be different. The magnitude of n_t depends on several factors such as net radiation, vegetation, snow cover, ground thermal properties, surface relief and subsurface drainage. The factors for different conditions are determined empirically and some typical values are reported in [13]. For the calculations here, the thawing factor value of $n_t = 1$ is assumed to be reasonable.

The volumetric latent heat *L* can be expressed as

$$L = \rho_d L_f \frac{w - w_u}{100} \tag{2.4}$$

where ρ_d is the dry density of the soil, L_f is the specific latent heat of fusion (the amount of energy absorbed when a unit mass of ice is converted into a liquid at the melting point; typically, 333.7 kJ/kg), w is the total water content and w_u is the unfrozen water content of the frozen soil. For soils with little or no unfrozen water (such as sands and gravels), the unfrozen water content is usually very small. For many practical problems, assuming $w_u = 0$ will give acceptable L values for the active layer thickness calculation.

The active layer thickness is calculated for the locations of interest in Longyearbyen based on the temperature data presented earlier and the Stefan Solution described above. Based on experimental

PROJECT NO. 102015174	REPORT NO. 2017:00656	VERSION 01	9 of 39



measurements at a selected location, the unfrozen thermal conductivity, the dry density and the total water content were estimated to be $\lambda_u = 1.8 \text{ W/m/K}$, $\rho_d = 1800 \text{ kg/m}^3$ and w = 30 %, respectively; [15]. The progression of the active layer thickness with time is shown in Figure 2-4. The air thawing indices based on inferred daily temperatures are used for the calculation.



Figure 2-4: Progression of active layer thickness with time.

It can be seen from the plot that the thickness of the active layer increases, corresponding to the air temperatures forecasts, from around 1 m in the present day to more than 2 m after several decades. The rising temperatures not only increase the thickness of the active layer but also increase the temperature in the permafrost. The warming of the permafrost is discussed in the following section.

2.3 Ground Temperature: Numerical Simulations

The evolution of the ground temperature with time is studied based on numerical simulations. The GeoStudio package Temp/W is used to perform these simulations. The model step, model conditions and results are discussed in the following sections.

Model Geometry and Mesh

A typical idealized slope geometry is used here for the thermal analyses. The slope angles vary at the different locations of interest in Longyearbyen. For the simulation of the ground thermal regime using Temp/W, the slope angle does not have an effect on the outputs. The dimensions of the idealized slope are shown in Figure 2-5.

The model is spatially discretized with an average element size of 0.5 m. As the current problem set up does not involve complex initial/boundary conditions and material properties, numerical problems are not anticipated and a uniform mesh size is used throughout the model.



Figure 2-5: Model geometry and mesh used for the representative thermal analysis.

Material Properties

A full thermal model is used to model the material properties in Temp/W. The material properties used are given in Table 1.

Parameter	Value	Unit
Unfrozen Thermal Conductivity	1.8	W/m/K
Frozen Thermal Conductivity	1.6	W/m/K
Unfrozen Specific Heat Capacity	3700	kJ/m ³ /K
Frozen Specific Heat Capacity	1440	kJ/m ³ /K
Dry Density of Soil	1800	kg/m ³
Total Water Content	30	%
Table 1. Material properties used for	n thormal analy	og in Tomn/M

 Table 1: Material properties used for thermal analyses in Temp/W.

For simplicity of the thermal analyses, a homogeneous soil body is assumed for the model here.

Initial Conditions

The simulations are aimed at showing the evolution of the ground temperatures in the active layer and the permafrost based on the predicted temperature data. To demonstrate this, the thermal analyses are performed for the period from 2001 - 2050. The air temperature data for the year 2000 is used to generate the initial conditions for the subsequent analyses. The daily mean air temperature data for the year 2000 is shown in Figure 2-6. The mean annual temperature is used as the activation temperature for the initial analyses.

Boundary Conditions

The existing air temperature data and forecast is applied as a thermal boundary condition at the ground surface. A step function is generated based on the seasonal mean temperatures for the targeted period of analysis. A plot of the step function for the period of analysis and a close-up for the first few years is shown in Figure 2-7. Natural thermal boundary conditions are assumed at the left, right and bottom boundaries of the model.









Figure 2-7: Thermal boundary condition based on seasonal mean temperatures as a step function for the period of analysis (top) and a close-up for the first three years (bottom).

Results

The ground temperature profiles for selected years are shown in terms of contour plots in Figure 2-8 to Figure 2-11. The figures are shown at the end of the thawing season for each year, where the time points vary depending on the temperature data of the year in question. We observe from the results that, as predicted by analytical calculations, the active layer thickness increases with time based on the temperature forecast. The results also show that the permafrost underneath the active layer gets warmer over the years. This gives an indication on the evolution of the ground thermal regime based on the simplified and homogenized analyses performed here. The trends of this evolution may be expected to

PROJECT NO. REPORT NO. 102015174 2017:00656	VERSION 1	L2 of 39
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be similar for various ground conditions in Longyearbyen. The temperature profiles versus depth for the selected years are shown in Figure 2-12.



Figure 2-8: Ground temperatures at the end of the thawing season in the year 2020.



Figure 2-9: Ground temperatures at the end of the thawing season in the year 2030.



PROJECT NO.	REPORT NO.	VERSION	13 of 39
102015174	2017:00656	01	15 01 55





Figure 2-11: Ground temperatures at the end of the thawing season in the year 2050.



Figure 2-12: Ground temperature profiles for selected years. The profiles are shown at time points when the thawing season ends and the next freezing period starts. These time points vary for the selected years depending on their respective temperature data.

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PROJECT NO.	REPORT NO.	VERSION	14 of 39
102015174	2017:00656	01	



3 Slope Stability Evaluation

The stability of a selected slope in Longyearbyen is studied. The effects of climate change and material properties are investigated and discussed in the following sections.

3.1 Location of Slope

The location of the slope selected for a case study is shown in Figure 3-1. The slope profile is extracted from [16] based on the cross-section line shown in the figure.



Figure 3-1: Location of slope and cross-section considered for a slope profile.

The stability of the slope is evaluated for changing climate by considering varying active layer thicknesses. Specifically, active layer thicknesses of 1.0 m, 1.5 m and 2.0 are considered and the models for these are shown in Figure 3-2, Figure 3-3 and Figure 3-4, respectively. The evaluations are performed using the software SLIDE which is based on limit equilibrium methods.

The material parameters used for the analyses are based on the index properties obtained from the project field and laboratory investigations. For drained analyses a cohesion of 3.5 kPa and a friction angle of 25° are assumed as reference values for the active layer. For the undrained case, a surface undrained shear strength of 5 kPa and a shear strength change with depth of 2 kPa/m are assumed as reference values. Conditions of excess pore pressure are simulated in a simplified and indirect manner by increasing the self-weight of water by 15%.

PROJECT NO. 102015174	REPORT NO. 2017:00656	VERSION 01	15 of 39



Figure 3-2: Slope profile with a 1.0m thick active layer thickness, including gravel berms and illustration of buildings.

PROJECT NO. 102015174	REPORT NO. 2017:00656	VERSION 01	16 of 39		



Figure 3-3: Slope profile with a 1.5m thick active layer thickness, including gravel berms and illustration of buildings.

PROJECT NO. 102015174	REPORT NO. 2017:00656	VERSION 01	17 of 39



Figure 3-4: Slope profile with a 2.0m thick active layer thickness, including gravel berms and illustration of buildings.

PROJECT NO. 102015174	REPORT NO. 2017:00656	VERSION 01	18 of 39



3.2 Effect of Climate Change

The effect of climate change is considered in terms of an increasing active layer thickness. Active layer thicknesses of 1.0 m, 1.5 m and 2.0 m are considered. For simplicity, the active layer thicknesses are assumed to have a uniform thickness along the slope profile; these may be slightly different under insulating conditions such as gravel berms. The variation of the factor of safety with active layer thickness under drained and undrained conditions is shown in Figure 3-5. A similar variation under sudden shear strength reduction is shown in Figure 3-6.



Figure 3-5: Factor of safety versus active layer thickness under drained and undrained conditions.



Figure 3-6: Factor of safety versus active layer thickness under sudden shear strength reduction due to precipitation or other instantaneous loading.

PROJECT NO.	REPORT NO.	VERSION	19 of 39
102015174	2017:00656	01	19 01 39



3.3 Sensitivity to Material Parameters

The effect of the key material parameters on the factor of safety is investigated through sensitivity analyses. The sensitivity of the factor of safety to the cohesion and friction angle, relevant for drained analyses, is shown in Figure 3-7. A similar plot illustrating the effects of undrained shear strength and its increment with depth is shown in Figure 3-8. The sensitivity analyses are performed with a 2 m active layer thickness as a reference.



Figure 3-7: Effects of the cohesion and friction angle of the active layer on factor of safety. The reference value of the friction is applied when varying the cohesion and vice versa.



Figure 3-8: Effects of the surface undrained shear strength of the active layer and its increment with depth on factor of safety. The reference value of the undrained shear strength is applied when varying its increment and vice versa.

Note that the safety factors reported so far are intended to give an indication of the effect of climate change and the variation of material parameters. Various assumptions are made in the calculations and the numbers should not be taken as explicitly conclusive. The observed trends are, however, expected to hold under different circumstances.

PROJECT NO.	REPORT NO.	VERSION	20 of 39
102015174	2017:00656	01	20 01 33



4 Laterally Loaded Piles on a Slope

Pile foundations may be subjected to lateral loading in various ways. One such way is the downward movement of soil on a slope for piles installed on a sloping ground. In cold regions, the downward movement of soil may be caused by a process known as solifluction, which is briefly discussed below. In subsequent sections, the capacity of piles subjected to such lateral loading is investigated through analytical calculations and numerical simulations.

4.1 Solifluction

Solifluction is defined as a slow downslope flow of saturated unfrozen earth materials according to the glossary of permafrost by [26] where one component could be creep of frozen ground. When the soil above the permafrost is thawed, which is the active layer, the water in the soil becomes trapped because the underlying permafrost is considered to be impermeable. This leads to oversaturation in the active layer and a downward slide occurs under the pull of gravity. The rate of solifluction may vary depending on several factors. Climate change affects the ground thermal regime through frequent freeze-thaw cycles and increased active layer thicknesses, thereby increasing the rate of solifluction. [27] claims that solifluction movements are a result of frost heaving and subsequent thawing and that creep is not a significant part of the process.

Infrastructure built on slopes susceptible to solifluction will be subjected to forces due to the downward movement of the soil in the active layer. Thus, the additional forces that results from solifluction should be accounted for in the design of these infrastructure.

For structures designed and built without considering the effect of solifluction, the serviceability during the life time of the structures must be investigated to take the necessary counter measures in the face of climate change.



Figure 4-1: Illustration of soil downward movement on a slope due to solifluction (top) and case study of flow around pile on a slope after [27] (bottom).

PROJECT NO.	REPORT NO.	VERSION	21 of 39
102015174	2017:00656	01	210133



A specific focus of the current study is buildings in Longyearbyen supported by pile foundations on sloping terrains. An illustration of the downward movement of soil on a slope where piles are installed is shown in Figure 4-1. We aim to investigate the effect of solifluction on the lateral capacity of piles. **The study is performed in a generic way such that the results can serve to assess the serviceability of existing buildings and add knowledge for the design of future buildings**. The theory of laterally loaded piles is first discussed and analytical and numerical calculations are then performed for piles on a slope subjected to lateral loads due to soil movement.

4.2 Theory of Laterally Loaded Piles

When a pile is subjected to lateral loading, the earth pressure distribution around the pile changes as illustrated in Figure 4-2. As the pile deflects, the stresses on the backside of the pile decrease whereas the stresses increase on the front, if there is no loss of contact between the pile and the soil.



Figure 4-2: A pile subjected to lateral loading and soil stress distribution around the pile before and after deflection.

Laterally loaded piles in soil are usually analysed by developing a nonlinear relationship between the soil resistance (p) and the pile head deflection (y), resulting in the so-called p-y curve. A beam model is usually used to develop this relationship. The general differential equation of this model is given by

$$E_p I_p \frac{d^4 y}{dz^4} + P_z \frac{d^2 y}{dz^2} + E_{py} y - Q = 0$$
(4.1)

where $E_p I_p$ is the bending stiffness of the pile, y is the lateral deflection, z is the depth along the pile, P_z is the axial load on the pile, E_{py} is the soil reaction modulus and Q is any distributed load along the length of the pile. The soil reaction modulus is obtained from a p-y curve as illustrated in Figure 4-3. For piles subjected to lateral loading due to a sliding soil, as in the case of solifluction, the beam model equation is modified to account for the movement of the soil. The modified equation is

$$E_p I_p \frac{d^4 y}{dz^4} + P_z \frac{d^2 y}{dz^2} + E_{py} (y - y_{soil}) - Q = 0$$
(4.2)

where $y - y_{soil}$ represents the relative pile-soil movement and E_{py} in this case is obtained from the *p*y curve adjusted for soil movement.

PROJECT NO.	REPORT NO.	VERSION	22 of 39
102015174	2017:00656	01	22 01 33





Figure 4-3: p-y curve in stable and sliding soil.

4.3 p-y Curves for Frozen Soil

The development of p-y curves is, in general, dependent on the soil type and loading conditions. It is usually assumed that the stress-strain curve for soil from experiments and the p-y curve of soil response have similar shapes. The first step in constructing p-y curves is to calculate the ultimate soil response per unit depth of pile length. This for frozen soil, according to [28], may be calculated from

$$p_{ult} = N_p cD \tag{4.3}$$

where N_p is the ultimate bearing capacity coefficient, c is the soil shear strength and D is the pile diameter or width. The bearing capacity coefficient increases with depth and may be calculated from

$$N_p = 3 + \frac{\sigma_v}{c} + \frac{Jz}{D} \tag{4.4}$$

where σ_v is the vertical overburden pressure at depth *z*, *J* is an empirical coefficient with a typical value of 0.5 and *z* is the depth below ground level. The *p*-*y* curve is then approximated by the parabola

$$p = \frac{1}{2} p_{ult} \left(\frac{y}{y_{50}}\right)^{\frac{1}{n}}$$
(4.5)

where p is the soil reaction to a lateral pile deflection, y is the lateral pile deflection and y_{50} is the lateral deflection at which $p = p_{ult}/2$ and n is a stress-strain exponent. The value of y_{50} can be approximately calculated from

$$y_{50} = 2.5\varepsilon_{50}D \tag{4.6}$$

where ε_{50} is the strain at one-half of the ultimate soil strength. A typical value of $\varepsilon_{50} = 0.25\%$ is used for the short-term strength and increased for the long-term depending on various factors. Suggested values of ε_{50} for fine- and coarse-grained soils may be referred from [28].

4.4 Analytical Calculations

The capacity of piles subjected to lateral loading is investigated here based on analytical approaches discussed previously. For the pile foundations of interest in this study, besides the type of lateral loading and soil type, one of the main factors that affects the pile capacities is climate change. This affects pile

PROJECT NO.	REPORT NO.	VERSION	23 of 39
102015174	2017:00656	01	25 01 55



foundations in various ways. Increasing active layer thicknesses associated with solifluction are expected to add to the lateral loading of piles. In addition, the continued warming of the permafrost is anticipated to affect the magnitude of the soil reaction. Slope angle is the other factor that affects the capacity of pile on installed on a sloping ground. These two factors are investigated quantitatively in the following sections.

4.4.1 Effect of Climate Change

The strength of frozen soil, as known, is strongly dependent on temperature and other temperature dependent volumetric properties. Increased ground temperatures and recurrent freeze-thaw cycles due to climate change increase the thickness of the active layer (as shown in earlier sections) and reduce the long-term strength of the frozen soil. This in turn results in the reduction of the ultimate capacity of piles in frozen soils.

In a Mohr-Coulomb type interpretation of soil shear strength, the soil cohesion and effective angle of internal friction are the key parameters. The shear strength of frozen soil τ_f can thus be written as

$$\tau_f = c_f + \sigma'_v \tan \phi_f \tag{4.7}$$

where c_f is the cohesion of frozen soil, σ'_v is the effective overburden stress and ϕ_f is the effective angle of internal friction of frozen soil. For frozen soils at very low temperatures, the effective friction angle is usually negligible as increasing volumetric ice content binds the soil particles together. On the other hand, the soil cohesion increases significantly with decreasing temperature and increasing volumetric ice content. Thus, the shear strength of frozen soils is mainly governed by the cohesive strength, especially for fine-grained soils.

The frozen cohesive strength may be expressed as a function of temperature and volumetric ice content. One such expression proposed by [29] is given by

$$c_f = c_t + \frac{\rho_w L_f}{T_f} \langle T_f - T \rangle^{1-\alpha} \left(\frac{n_o - w_u}{n_o} \right)^{\beta}$$

$$\tag{4.8}$$

where c_t is the thawed cohesion, ρ_w is the density of water, L_f is the latent heat of fusion, T_f is the reference freezing temperature, T is the actual temperature, n_o is the initial porosity, w_u is the unfrozen water content and α and β are model parameters. For frozen soils where the unfrozen water content is negligible, the equation reduces to

$$c_f = c_t + \frac{\rho_w L_f}{T_f} \langle T_f - T \rangle^{1-\alpha}$$
(4.9)

An illustration of the cohesive strength of frozen soil versus temperature is shown in Figure 4-4. The plots are made by assuming $c_t = 20$ kPa, $\rho_w = 1000$ kg/m³, $L_f = 334$ kJ/kg, $T_f = 273.15$ K, $n_o = 0.4$, $w_u = 0.05$ and $\beta = 3.0$. The cohesion increases significantly with decreasing temperature. The plot illustrates that warming of permafrost is associated with a drop in cohesive strength.

PROJECT NO. REPORT NO. VERSION 24 of 3 102015174 2017:00656 01 24 of 3				
	PROJECT NO. 102015174	REPORT NO. 2017:00656	VERSION 01	24 of 39





Figure 4-4: Cohesive strength of frozen soil as a function of temperature.

As discussed previously, the ultimate soil reaction in cohesive soils is proportional to the shear strength of the soil. This results in a significant difference in the p-y curves for the active layer and the permafrost underneath. A typical p-y curve at a certain depth in the active layer is shown in Figure 4-5. A pile diameter of 0.14 m is assumed for this and subsequent results, unless otherwise specified. The pile under lateral loading deflects the most within the active layer and this is reflected in the magnitude of the soil reaction given for the assumed cohesion and overburden stress. An increased active layer thickness implies an increased region of weak layer which may result in larger pile deflections for the same lateral loading.



Figure 4-5: A typical p-y curve in the active layer (thawed soil).

PROJECT NO.	REPORT NO.	VERSION	25 of 39
102015174	2017:00656	01	25 01 55



Figure 4-6 shows *p*-*y* curves for permafrost at different temperatures. The plots are made at a similar depth, for the same overburden stress, and assuming the same pile geometry. The lateral force required to cause the same level of deflection decreases with increasing temperature.



Figure 4-6: Permafrost p-y curves at different temperatures under similar conditions of overburden stresses and pile cross-sectional geometries.

4.4.2 Effect of Slope Angle

For piles installed on sloping terrains, the slope angle affects the ultimate lateral capacity and thus the resulting p-y curves. The effect of the slope angle on the ultimate pile capacity, according to [30], may be taken into account through

$$p_{ult} = N_p c D \left(\frac{1}{1 + \tan \theta}\right) \tag{4.10}$$

where θ is the slope angle. In the expression above, it is assumed that the soil in the active layer is finegrained and the effect of cohesion is more significant compared to the effect of friction angle, which is negligible for frozen soils at very low temperatures.

The effect of slope angle on p-y curves is illustrated in Figure 4-7 for soil properties in the active layer. A significant reduction is observed in the ultimate pile capacity as the slope angle increases.

PROJECT NO. 102015174	REPORT NO. 2017:00656	VERSION 01	26 of 39





Figure 4-7: Effect of slope angle on the lateral capacity of piles. The plots are made for thawed soil properties corresponding to a typical active layer.

The ultimate pile capacity in permafrost also reduces with increasing slope angle, as shown in Figure 4-8. The shear strength of permafrost at different temperatures is considered with other factors being in a similar condition.



Figure 4-8: Effect of slope angle on the ultimate lateral capacity of piles in permafrost at different temperatures. The comparisons are made under similar conditions of overburden stress and pile cross-sectional geometries.

PROJECT NO.	REPORT NO.	VERSION	27 of 39
102015174	2017:00656	01	27 01 33



4.4.3 Effect of Pile Diameter

For fine-grained soils, the ultimate soil reaction under lateral loading, as expected, is proportional to the pile diameter or width. The effect of pile diameter on soil response in the active layer is illustrated through the p-y curves in Figure 4-9.



Figure 4-9: Effect of pile diameter on the lateral capacity of piles.

4.5 Finite Element Simulations

It was shown through analytical calculations in the previous section that factors such as climate change, slope angle and pile geometry affect the lateral capacity of piles in frozen slopes. Finite element simulations are performed here to further study some aspects of these factors. In particular, the effect of climate change is considered through varying the active layer thickness with piles on slopes. The downward movement of soil due to solifluction is taken into account and the effect of this on the capacity of piles installed at different locations on a slope is investigated. The finite element software PLAXIS 2D is used for the simulations. The combined effect of these factors is analysed by quantifying pile head deflections and structural forces.

Model Geometry and Mesh

A numerical model with an arbitrary slope is setup with single piles at the middle and the toe of the slope. The model dimensions and the finite element meshes used for the analyses are shown in Figure 4-10, Figure 4-11 and Figure 4-12 for active layer thicknesses of 1.0m, 1.5m and 2.0m, respectively.

PROJECT NO.
102015174





Figure 4-10: Finite element model dimensions and mesh with a 1.0 m thick active layer.



Figure 4-11: Finite element model dimensions and mesh with a 1.5 m thick active layer.



Figure 4-12: Finite element model dimensions and mesh with a 2.0 m thick active layer.

PROJECT NO. REPORT NO. 102015174 2017:00656	VERSION 01	29 of 39
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Axial loads are applied at the top of the piles to simulate the loads transferred from the superstructure to the foundation. For a typical residential house, the axial load transferred to a single pile is estimated to be in the range 50 - 100 kN, depending on the number of piles used for support. An axial load of 50 kN is assumed to act on a single pile for the simulations here.

Material Properties

The active layer and the permafrost underneath it are modelled using the Mohr-Coulomb model. For simplicity, the main material parameters are averaged for the layers. The temperature of the permafrost is considered in the estimation of its shear strength properties. We have seen earlier that the permafrost gets warmer as the active layer thickness increases, thus reducing its shear strength.

The piles are modelled using a linearly elastic material. Square hollow steel piles are commonly used nowadays for construction of buildings in Longyearbyen, [15]. A width of 140 mm and a wall thickness of 8 mm are used for the pile dimensions. The piles are assumed to be embedded up to 5 m in the permafrost. The Young's modulus and Poisson's ratio of steel are set to 200 GPa and 0.3, respectively. The stiffness of the pile is reduced in the input considering that the simulations are performed in 2D plane strain; see [31].

Model Conditions

We aim to investigate the lateral loading on piles due to the downward movement of the active layer i.e. solifluction. Solifluction is a time dependent process and the rate of downward movement at a certain location varies depending on several factors. It is anticipated that the maximum rates of solifluction occur during the thawing season when the active layer thickness is at its maximum resulting in the highest build-up of excess pore pressure in the soil. The excess pore pressure is dissipated gradually and this decreases the rate of solifluction afterwards. For the active layer thicknesses of 1.0 m, 1.5 m and 2.0 m considered here, downward movement of the soil on the slope is initiated by introducing a thin weak shear zone between the active layer and the permafrost.

Two pile locations, one at middle of the slope and one at the toe, are considered. A pile at the crest is not considered here; the maximum lateral force exerted on a pile at the crest will be in the same order or lesser than on a pile at mid slope depending on where downward movement is initiated; see [32].

Results

The results from the analyses are presented in the following in terms of pile head deflections and bending moments in the pile. These are discussed based on climate change and pile location on slope as the main factors.

4.5.1 Effect of Climate Change

In the event of the downward movement of soil on a sloping terrain, higher active layer thicknesses are clearly associated with a larger sliding soil mass. Thus, the lateral force exerted on the pile foundations increases with increasing active layer thicknesses, resulting in larger pile deflections and pile internal forces. These are quantified for the toe and mid piles in Figure 4-13 and Figure 4-14, respectively, for the three active layer thicknesses considered.

If the 1.0 m thick active layer is taken as a reference, a 50% increase in the active layer thickness results in approximately tripled pile head deflections, both for the toe and mid piles. On the other hand, a 100% increase in the active layer thickness results in more than a fivefold increase in the deflections of the toe and mid piles. The bending moments in the piles also increase corresponding to the increase in deflections. These findings are based on square hollow steel piles of the assumed dimensions used for

PROJECT NO.	REPORT NO.	VERSION	30 of 39
102015174	2017:00656	01	50 01 59



the simulations. Similar rates of increase may be expected for piles made from other materials or having different cross-sectional geometries.



Figure 4-13: Steel piles - head deflections and bending moments of the toe pile under different active layer thicknesses.

4.5.2 Effect of Pile Location

The location of the pile determines the magnitude of lateral force sustained by the pile during the downward movement of soil. The lateral forces on piles installed at the middle of the slope are larger than on piles installed at the toe of the slope. These are again shown in terms of deflections and bending moments in Figure 4-13 and Figure 4-14 for the toe and mid piles, respectively. Under the same conditions of material properties and pile geometries, the calculations here show that the pile at mid slope experience nearly doubled deflections and internal forces compared to the pile at the toe of the slope. Similar observations are expected to hold for different materials and pile properties. As discussed earlier, piles installed close to the crest of the slope are expected to experience varying lateral forces, up to the same order of magnitude as piles at mid slope, depending on where the downward movement of the soil is initiated.

4.5.3 Effect of Pile Material

A similar set of analyses are performed for piles made of timber. A circular cross-section with a diameter of 250 mm is assumed for the piles. The Young's modulus and Poisson's ratio of timber are set to 10 GPa and 0.3, respectively.

The head deflections and bending moments for the timber pile considered are shown in Figure 4-15 and Figure 4-16, for the toe and mid piles, respectively. We observe that the head deflections are significantly larger for timber piles when compared to steel piles, which is expected due to the lower Young's modulus of timber.

PROJECT NO. 102015174	REPORT NO. 2017:00656	VERSION 01	31 of 39





Figure 4-14: Steel piles - head deflections and bending moments of the mid pile under different active layer thicknesses.



Figure 4-15: Timber piles - head deflections and bending moments of the toe pile under different active layer thicknesses.

PROJECT NO. 102015174	REPORT NO. 2017:00656	VERSION 01	32 of 39





Figure 4-16: Timber piles - head deflections and bending moments of the mid pile under different active layer thicknesses.

4.6 Bending Capacity of Piles

The failure mode of piles subjected to lateral loading depends on various factors such as the property of the soil, the geometry of the pile and the type of end fixity. Piles may be free-headed or restrained (fixed head) depending on the type of fixity at the top of the pile. Figure 4-17 shows the common failure modes of free-headed piles, which could occur either through the development of plastic hinges due to bending beyond the yield stress of the material or excessive translational or rotational deformations. Similar failure modes for restrained piles are shown in Figure 4-18 where the plastic hinges may develop at multiple locations.



Figure 4-17: Failure modes for free-headed piles: Long piles – usually through development of plastic hinges due to bending (left) and Short piles – excessive deformation (right), after [33].

PROJECT NO.	REPORT NO.	VERSION	33 of 39
102015174	2017:00656	01	55 01 55





Figure 4-18: Failure modes for restrained piles through excessive deformation (left) and development of plastic hinges (centre and right), after [33].

Failure modes with plastic hinges occur when the ultimate flexural strength or yield stress of the material is exceeded. For piles installed in frozen ground with a stiff permafrost layer and a seasonally changing active layer, failure modes with plastic hinges may occur for sufficiently embedded piles. The maximum moment which can be carried by the pile cross-section without exceeding the yield stress must be checked. From beam theory, this maximum yield moment is given by

$$M_y = \frac{\sigma_y I_p}{z} \tag{4.11}$$

where σ_y is the yield stress of the material, I_p is the moment of interia of the pile and z is the distance from the neutral axis to the extreme tension or compression fibre. For a circular cross-section, the moment of inertia is given by

$$I_p = \frac{\pi d^4}{32} \tag{4.12}$$

If the yield stress of timber is assumed to be $\sigma_y = 40$ MPa and if a material factor of 0.8 is introduced, the yield moment versus pile diameter plot shown in Figure 4-19 is obtained. A timber pile with a diameter of 250 mm, as considered in the simulations earlier, yields at a bending moment of around 49 kN m under these conditions.





PROJECT NO.	REPORT NO.	VERSION	34 of 39
102015174	2017:00656	01	34 01 33



One of the major challenges with timber piles is the problem of aging where structural capacity is lost due to rotting. A simple evaluation of such a capacity loss can be made by assuming that rotting reduces the effective diameter of the pile against bending and shear. If we introduce a factor α (in percentage) to represent such a capacity loss, the yield moment of a rotten pile in terms of the capacity of the original pile may be expressed as

$$M_{\nu,r} = (1 - \alpha)^3 M_{\nu} \tag{4.13}$$

where $M_{y,r}$ represents the yield moment of the rotten pile. Figure 4-20 illustrates the capacity reduction of timber piles due to aging according to the assumptions made here.



Figure 4-20: Bending capacity reduction of round timber piles due to aging.

PROJECT NO. 102015174	REPORT NO. 2017:00656	VERSION 01	35 of 39



5 Summary, Conclusions and Outlook

The effect of climate change on existing infrastructure in Longyearbyen, Svalbard is investigated in this study. Climate data recordings show that, over the past couple of years, record-breaking temperature and precipitations measurements are observed in this area. It is anticipated that this will pose a serious threat to existing infrastructure. Adaptations of these infrastructure to changes in climate for safety and serviceability is of paramount importance. The current study aims to contribute towards this initiative.

The particular focus of the study was slopes and buildings supported on sloping terrains in Longyearbyen. Changes in ground temperature are investigated based on existing temperature data and forecasts. The ground thermal regime is then used to evaluate the stability of representative slopes in the study area. The capacity of single piles on a slope is also investigated by considering various factors such as slope angle, location of pile on slope, pile material and geometry. The following findings are observed from the investigation:

- The projected climate data show that temperatures will keep rising in Svalbard. Based on the analytical and numerical studies performed for the projected temperature data, it is observed that the active layer thickness will increase up to 2 m or more, depending on the thermal properties of the soil. The increase in ground temperatures also results in the warming of the permafrost underneath the active layer. The stability of slopes and the bearing capacity of existing infrastructure foundations is expected to be significantly affected by these changes.
- Slope stability evaluations were performed for a representative slope in the study area by considering changing active layer thicknesses according to the projected ground temperature regime. The factor of safety against slope failure decreases with increasing active layer thickness. Under the specific assumptions made for the evaluation, the representative slope was found to be stable for active layer thicknesses of up to 2m. Sensitivity analyses show that the factor of safety is significantly affected by changes is material parameters such as cohesion and friction angle, which are associated with the ground thermal regime. Accurate estimation of material properties is required for a definitive slope stability evaluation.
- The performance of single piles on a slope is investigated by performing various analytical and numerical studies. One of the effects of an increase in active layer thickness on sloping terrains is the risk of solifluction, which is a slow downward movement of soil. The soil movement exerts additional lateral forces on pile foundations, affecting the ultimate capacity of the piles. This is especially significant for building where the effect of solifluction is not considered in the original design. It is observed from the analyses that piles subjected to such additional lateral forces will experience increased deflections and internal forces. The deflections and internal forces increase with increasing slope angles and active layer thicknesses. Piles located in the middle of the slope are observed to experience larger deflections and internal forces is especially critical for timber piles where the capacity is expected (and shown) to reduce with aging.

Based on the observation from the current study, it is recommended to perform specific case studies for selected locations. Examples of specific selections for case study may be building located on steep slope angles and supported by timber piles. Additional field and laboratory measurements may be performed for a selected site with instrumentation such as piezometers and inclinometers. Investigations with these instruments will provide data on the dynamics of solifluction processes and pore pressures at the given location. Specific and detailed computer simulations may then be performed for the instrumented sites.

In general, the study here highlights the importance of assessing the effect of climate change on existing infrastructure to ensure safety and serviceability. The knowledge gained from the study also highlights the necessity of the consideration of climate change in the design of new infrastructure to be built in affected areas.

PROJECT NO.	REPORT NO.	VERSION	36 of 39
102015174	2017:00656	01	50 01 55



Acknowledgements

The financial support for this study from Svalbard Miljøvernfond, Longyearbyen Lokastyre and Store Norske Spitsbergen Kulkompani AS is greatly acknowledged. We would like to thank Rasmus E. Benestad from The Norwegian Meteorological Institute for providing climate data used in the study.

Report information

Svalbard's Miljøvernfond project number: 16/87. SINTEF project number: 102015174. RiS database project number: 10968.

PROJECT NO. 102015174	REPORT NO. 2017:00656	VERSION 01	37 of 39



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PROJECT NO.	REPORT NO.	VERSION	38 of 39
102015174	2017:00656	01	30 01 33

SINTEF

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PROJECT NO.	REPORT NO.	VERSION	39 of 39
102015174	2017:00656	01	



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